

Introduction to Computer Science

Tutorial 9: Functions

1. Some Arithmetic Functions

In a C file, define the following functions:

1. `int square(int)` that calculates the mathematical function $x \rightarrow x^2$.
2. `int abs(int)` that calculates the function $x \rightarrow \{-x \text{ if } x < 0, x \text{ otherwise}\}$.
3. `int max(int, int)` that calculates the function $(x,y) \rightarrow \{x \text{ if } x > y, y \text{ otherwise}\}$.
4. `int maxAbs(int, int)` that calculates the function $(x,y) \rightarrow \{|x| \text{ if } |x| > |y|, |y| \text{ otherwise}\}$. The definition of `maxAbs` should not use any conditional statement or operator, and should use call the previous functions `abs` and `max`.

Write a main function that allows you to test your functions.

2. Prime Numbers and Fibonacci Numbers

2.1 Define a function `int isPrime(int n)` that returns 1 if n is a prime and 0 otherwise.

Write a main function that reads an integer from standard input, and checks whether it is a prime number, showing the result of the check on standard output.

2.2 Write a function `int fibonacci(int n)` that returns the n th Fibonacci number. Write a main function that reads an integer n from standard input, prints out the n -th Fibonacci number on standard output.

2.3 Write a program that reads an integer n from standard input (or, better, as a command line argument), and finds the positive integers smaller or equal to n that are at the same time Fibonacci numbers and prime numbers.

3. Goldbach Conjecture

The Goldbach conjecture says that every even integer n greater than 2 is the sum of two prime numbers. Computers have been used extensively to test this conjecture. No counterexample has ever been found.

Write a C program that will test that the conjecture for all even integers between n and m , positive integers received from standard input. Your output must show, for each even integer, if decomposable as two primes, the two that lead to the number. For instance:

$$\begin{array}{l} 700 = 17 + 683 \\ 702 = 11 + 691 \end{array}$$

4. Strings

4.1 Design and implement in C a program that receives two strings from standard input (or from the command line, would be better), and decides whether these strings are anagrams.