

Introduction to Computer Science

Lecture 9

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(based on material by Guillaume Hoffmann)

Today

- Functions
- The return statement
- Function prototypes
- Call-by-value

The big picture

- **Problem decomposition**: taking a problem and breaking it into small, manageable pieces is critical to writing large programs.
- Imperative programming languages typically provide *subroutines* (in C, **functions**) to decompose programs into smaller functional components.
- A program will now consist of one or more functions, one of them being `main()`.
- Program execution begins with `main()`
- `main()` can *call* other functions, including library functions such as `printf()`, `rand()`.
- Functions use program variables, whose access is determined by **scope rules**.

Function Definition

- General form:

```
type function_name( parameter list ) { declarations statements }
```

- Everything before the first brace is the *header* of the function.
- Everything between the braces is the *body* of the function definition.
- The parameter list is a comma-separated list of declarations.

```
int factorial(int n) {  
    int product = 1;  
    for (int i = 2; i <= n; i++) {  
        product = product * i  
    }  
    return product;  
}
```

Detailed description of the example

- A definition alone does not execute anything. The function needs to be **called** for something to happen.
- Evaluating expression `factorial(7)` causes a call.
- The effect is to execute the code in the function definition, with `n` having the value 7.

The value returned by the function has type int

The parameter list here is the declaration `int n`. The function has a single parameter of type int.

```
int factorial(int n) {  
    int product = 1;  
    for (int i = 2; i <= n; i++) {  
        product = product * i  
    }  
    return product;  
}
```

Function definition/call example

It does not return any value

It does not have any parameters

```
void wrt_address(void) {  
    printf("%s\n%s\n%s\n%s\n%s\n\n",  
        "*****",  
        "** SANTA CLAUS **",  
        "** NORTH POLE **",  
        "** EARTH **",  
        "*****");  
}
```

- Evaluating expression `wrt_address()` causes function to be called.

```
int main() {  
    for (int i = 0; i < 3; i++) {  
        wrt_address();  
    }  
    return 0;  
}
```

Function Parameters and Local Variables

- In the definition, the name of the function is followed by a parenthesized list of **parameter declarations**.
- Parameters act as placeholders for values that are passed when the function is called.
- Sometimes, to emphasize their role as placeholders, these parameters are called the **formal parameters** of the function.
- The **function body** is a block and it may contain declarations of **local variables**.

```
int twice(int x) {  
    return (2 * x);  
}
```

```
int add(int a, int b, int c) {  
    int sum = a + b + c;  
    return sum;  
}
```

One job, one function

- Designing programs as collections of functions is essential for dealing with complexity.
- If programs are adequately separated into functions, it can become easier to reason about single functions and their behavior
- Both the writing and debugging are made easier.
- It is also easier to maintain or modify programs modularized into functions.
- We can change just the set of functions that need to be rewritten and expect the rest of the code to work correctly.
- Functions should be clear, readable and self documenting.
 - It is important that each function has a single responsibility.
 - It is important to choose adequate names for functions, that reflect their behavior

The return statement

- The `return` statement may or may not include an expression.
- The expression being returned can be enclosed in parentheses, but this is not required.
- When a `return` statement is encountered, execution of the function is terminated and control is passed back to the calling environment.
- If the `return` statement contains an expression, then the value of the expression is passed back to the calling environment as well.

```
return;  
return ++a;  
return (a * b);
```

Return Statements and Returned Values

- There can be zero or more return statements in a function.
- If there is zero, control comes back to calling environment at the end of the function body.
- Even if a function returns a value, a program does not need to use it:

```
getchar();    // get a char and do nothing with it  
c = getchar(); // get a char and assign it to c
```

Function prototypes

- Like variables, C requires functions to be declared before they are used.
- The syntax to declare a function is called the **function prototype**.
- A prototype tells the number and type of arguments that are passed to the function and the type of the value that is to be returned by the function.
- Example: `char toUpper(char);`
- This tells that `toUpper` is a function that takes a single argument of type `char` and returns a `char`.

Example of top-down design: creating a table of powers

```
#define N 7

long power(int, int);
void prn_heading(void);
void prn_tbl_of_powers(int);

int main(void) {
    prn_headin();
    prn_tbl_of_powers(N);
    return 0;
}
```

```
void prn_heading(void) {
    printf("\n::::: A TABLE OF POWERS :::::\n\n");
}

void prn_tbl_of_powers(int n) {
    int i, j;
    for (i = 1; i <= n; ++i) {
        for (j = 1; j <= n; ++j) {
            if (j == 1) {
                printf("%ld", power(i, j));
            }
            else {
                printf("%9ld", power(i, j));
            }
        }
        putchar('\n');
    }
}
```

```
long power(int m, int n) {
    int i;
    long product = 1;
    for (i = 1; i <= n; ++i) {
        product = product * m;
    }
    return product;
}
```

Here is the output of the program:

::::: A TABLE OF POWERS :::::

1	1	1	1	1	1	1
2	4	8	16	32	64	128
3	9	27	81	243	729	2187
....						

Alternative Style

- Because function definitions also serve as function prototypes, an **alternative style** is to remove the prototypes and to put the definitions before the calls.
- This makes `main()` go last.

```
long power(int m, int n)
{
}

void prn_tbl_of_powers(int n)
{
    .....
    printf("%ld", power(i, j));
    .....
}

int main(void)
{
    prn_heading();
    prn_tbl_of_powers(N);
    return 0;
}
```

Call-by-value

- Functions are invoked by writing their name and an appropriate list of arguments within parentheses.
- These arguments match in number and type (or compatible type) the parameters in the parameter list in the function definition.
- All arguments are passed “by value”. This means that each argument is evaluated, and its value is used locally in the execution of the function.
- In particular, **a variable itself is actually not passed to a function, what is passed is its value.**
- So, a function does not modify a variable, if this is passed as argument to the function from the calling environment.

Example

```
int compute_sum(int n);

int main(void) {
    int n = 3, sum;

    printf("%d\n", n);
    sum = compute_sum(n);
    printf("%d\n", n);
    printf("%d\n", sum);
    return 0;
}
```

```
int compute_sum(int n) {
    int sum = 0;
    while (n > 0) {
        sum = sum + n;
        --n;
    }
    return sum;
}
```

Function Call Summary

- Each expression in the parameter list is evaluated.
- Each value is assigned to its corresponding formal parameter at the beginning of the body of the function.
- The body of the function is executed.
- If a return statement is reached, it is executed and the control is passed back to the calling environment.
- If the return statement includes an expression, it is evaluated and that value is passed back to the calling environment too.
- If no return statement is reached, control is passed back to the calling environment when the end of the body of the function is reached.

Summary

- Functions help structuring C programs. They help breaking down a problem into smaller subproblems, each solved by a corresponding function.
- A return statement ends the execution of a function and passes the control back to the calling environment. If the return statement contains an expression as well, then the value of that expression is passed back as well.
- A function prototype tells the compiler the type and number of its parameters and the type of its returned value. If there are no parameters, the word void is used; if the function returns no value, void is also used as return type.
- Arguments to functions are passed by value in C. They must be type compatible with the corresponding types specified in the function prototype or definition.

Recursion

A recursive definition is the definition of a concept in terms of itself

Recursion in algorithms:

- Natural approach to solve many computational problems
- A *recursive algorithm* uses itself to solve one or more smaller identical problems

Recursion in programming languages:

- Recursive functions implement recursive algorithms
- A *recursive function* includes a call to itself

The structure of a recursive definition

A recursive definition must involve:

- **Base cases**, simple cases in the definition that do not define the concept in terms of itself
- **Recursive cases**, cases whose definition is given in terms of simpler instances of the same concept

Every recursive case must eventually reach a base case.

Components of a Recursive Algorithm

1. What is a smaller *identical* problem(s)?

 Decomposition

2. How are the answers to smaller problems combined to form the answer to the larger problem?

 Composition

3. Which is the smallest problem that can be solved easily (without further decomposition)?

 Base/stopping case

An example: Factorial numbers

A classical example of a recursive definition in Mathematics is the definition of a factorial numbers:

- **Base case:** Factorial of one is one:

$$1! = 1$$

- **Recursive case:** Factorial of a number n greater than one is n times the factorial of $(n-1)$:

$$n! = n \times (n - 1)!, \text{ provided } n > 1$$

Factorial function

```
int factorial(int n) {  
    if (n <= 0) return -1;  
    else {  
        if (n == 1) {  
            return 1;  
        }  
        else {  
            return n * factorial(n - 1);  
        }  
    }  
}
```

```
int main()
{
    printf("The factorial of 3 is: %d\n", 6);
    return 0;
}
```

(n receives 3)

returns 6

```
int factorial(int n) {
    if (n <= 0) return -1;
    else {
        if (n == 1) {
            return 1;
        }
        else {
            return n * 2;
        }
    }
}
```

(n receives 2)

returns 2

```
int factorial(int n) {
    if (n <= 0) return -1;
    else {
        if (n == 1) {
            return 1;
        }
        else {
            return n * 1;
        }
    }
}
```

(n receives 1)

returns 1

```
int factorial(int n) {
    if (n <= 0) return -1;
    else {
        if (n == 1) {
            return 1;
        }
        else {
            return n * factorial(n - 1);
        }
    }
}
```

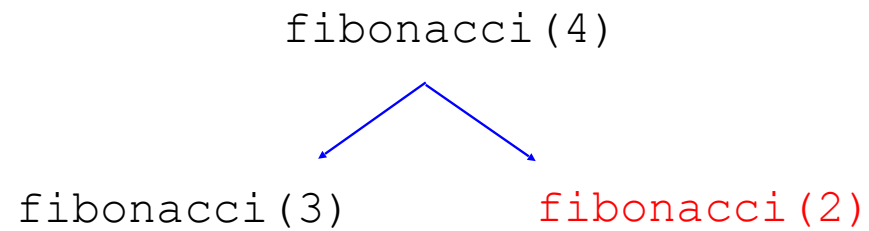
Fibonacci Numbers

- The numbers in the Fibonacci sequence can also be recursive defined:
- The n-th Fibonacci number is:
 - n , if $n \leq 1$
 - The sum of the two previous Fibonacci numbers, if $n > 1$:
 - $\text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2)$

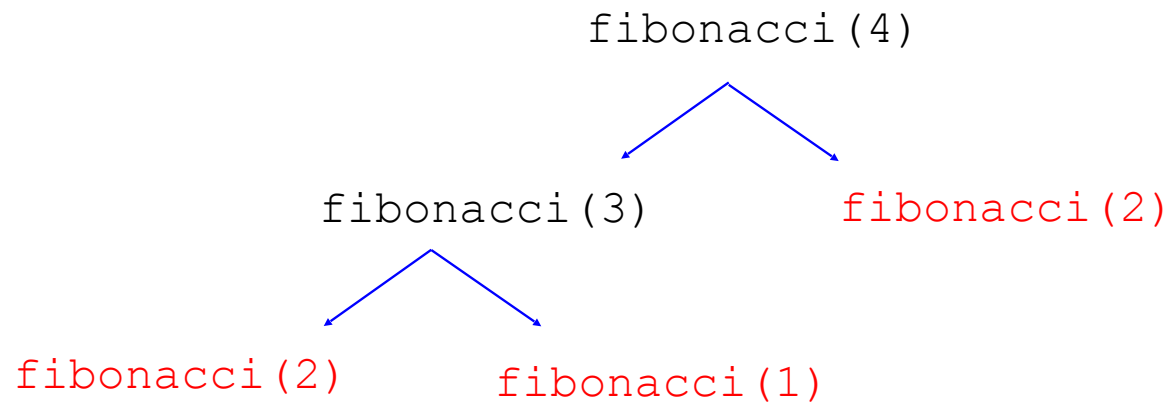
Fibonacci function

```
int fibonacci(int n) {  
    if (n <= 2) return n - 1;  
    else {  
        return fibonacci(n - 1) + fibonacci(n - 2);  
    }  
}
```

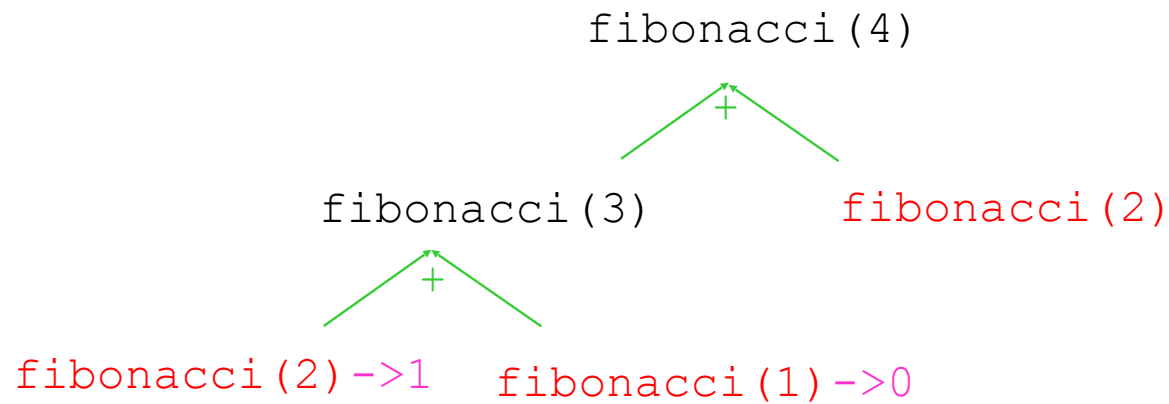
Execution Trace (decomposition)



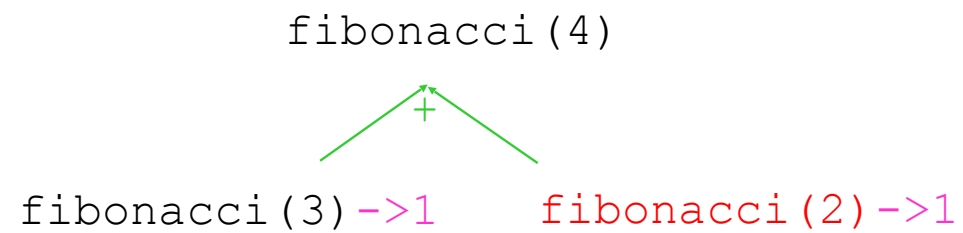
Execution Trace (decomposition)



Execution Trace (**composition**)



Execution Trace (**composition**)



Execution Trace (**composition**)

`fibonacci(4) -> 2`

Crucial aspects of a recursive function

- Case-based definitions
 - Using if-else statement (or some other branching statement)
- Some branches perform recursive calls (recursive cases):
 - "smaller" arguments or solve "smaller" versions of the same task (*decomposition*)
 - Combine the results (*composition*) [if necessary]
- Other branches: no recursive calls
 - stopping cases or base cases

Template

```
... rec_func (...)  
{  
    if ( ... ) // base case  
    {  
    }  
    else // decomposition & composition  
    {  
    }  
    return ... ; // if not void method  
}
```


Is this correct?

```
public static int factorial(int n)
{
    return factorial(n - 1) * n;
}
```

Infinite recursion

- Infinite Recursion
 - Incorrectly defined recursive solution
 - No decomposition (recursive calls are not on smaller problem instances)
 - Base cases may exist, and not be reachable
 - (Insufficient base cases, incorrectly defined decomposition)
 - No base case
- *Stack*: keeps track of function calls
 - Method begins: add function local data onto the stack
 - Method ends: remove function local data from the stack
- Recursion never stops; stack eventually runs out of space
 - **Stack overflow error**

Number of Zeros in a positive number

- Example: 2030 has 2 zeros
- If n is smaller than 10, it has no digits
- If n is greater than 10 (i.e., it has two or more digits):
 - the **number of zeros** is the **number of zeros** in n with the last digit removed
 - plus an additional 1 if the last digit is zero
- Examples:
 - number of zeros in 20030 is number of zeros in 2003 plus 1
 - number of zeros in 20031 is number of zeros in 2003 plus 0

recursive

zero_count function

```
int zero_count(int n) {  
    if (n < 10) {  
        return 0;  
    }  
    else {  
        int prefix_count = zero_count(n / 10);  
        if (n % 10 == 0) {  
            return prefix_count + 1;  
        }  
        else {  
            return prefix_count;  
        }  
    }  
}
```

Summary

- Recursive function: a function that calls itself
- Very powerful algorithm design technique
- Recursive algorithm design:
 - Decomposition (smaller identical problems)
 - Composition (combine results)
 - Base case(s) (smallest problem, no recursive calls)
- Implementation
 - Conditional (e.g. if-then-else) statements to separate different cases
 - Avoid infinite recursion
 - Make sure recursive calls are on smaller problem instances (decomposition)
 - Base cases must exist and be reachable from all (valid) function calls